

SWIFT J1749.4–2807: A neutron or quark star?

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Abstract We investigate an unique accreting millisecond pulsar with X-ray eclipses, SWIFT J1749.4–2807 (hereafter J1749), and try to limit the binary system by various methods including that of the Roche lobe, the mass-radius relations of both a main sequence (MS) and a white dwarf (WD) companion stars, as well as the measured mass function of the pulsar. The calculations are based on the assumption that the radius of the companion star has reached its Roche radius (or at 90%), but the pulsar’s mass has not been assumed to be a certain value. Our results are as follows. The companion star should be a MS. For the case that the radius equals to its Roche one, we have a companion star with mass $M \simeq 0.51M_{\odot}$ and radius $R_c \simeq 0.52R_{\odot}$, and the inclination angle is $i \simeq 76.5^{\circ}$; for the case that the radius reaches 90% of its Roche one, we have $M \simeq 0.43M_{\odot}$, $R_c \simeq 0.44R_{\odot}$ and $i \simeq 75.7^{\circ}$. We also obtain the mass of J1749, $M_p \simeq 1M_{\odot}$, and conclude that the pulsar could be a quark star if the ratio of the critical frequency of rotation-mode instability to the Keplerian one is higher than ~ 0.3 . The relatively low pulsar mass (about $\sim M_{\odot}$) may also challenge the conventional recycling scenario for the origin and evolution of millisecond pulsars. The results presented in this paper are expected to be tested by future observations.

Key words: X-rays: binaries, binaries: eclipsing, pulsar: general, individual: SWIFT J1749.4-2807

1 INTRODUCTION

One of the daunting challenges nowadays is to understand the fundamental strong interaction between quarks in the low-energy limit, i.e., the non-perturbative QCD (quantum chromo-dynamics). This unsolved problem results in the uncertainty to determine the nature of pulsar-like compact stars: either normal neutron stars or quark stars (e.g., Lattimer & Prakash 2004; Xu 2009). Nevertheless, compact stars may provide as astrophysical laboratories to understand the non-perturbative QCD in turn, and the pulsar mass and radius distribution would have important implications for the nature of pulsar and for the states of matter at supra-nuclear density. Certainly it is a very difficult task to determine precisely the masses of pulsars even in binary systems because of unknowing inclination angle, unless for general relativistic binaries in which many post-Keplerian parameters observed are applied.

An amazing system, SWIFT J1749.0-2807 provides us a perfect opportunity for measuring the mass of pulsar. J1749 is in a binary system, and the pulsar is in the phase of accreting matter from and is also eclipsed by its companion star. It was discovered in June 2, 2006 (Schady et al. 2006). J1749 is the first eclipsing accretion-powered millisecond X-ray pulsar (AMXP) system. Observations set an upper limit distance to this system of 6.7 ± 1.3 kpc (Wijnands et al. 2009). The rotation period of the pulsar is $\simeq 1.93$ ms and the eclipse by the companion star centered at the orbital phase of superior conjunction of the

Table 1 The timing parameters of J1749 to be used in our calculations, taken from Table 1 of Altamirano et al. (2010)

Parameter	Value
Orbital Period, P_{orb} (days)	0.3673696(2)
Projected semi major axis, $a_p \sin i$ (lt-s)	1.89953(2)
Eccentricity, e (95% c.l.)	$< 2 \times 10^{-5}$
Spin frequency 1st overtone, ν_0 (Hz)	1035.8400279(1)
pulsar mass function, f_p (M_\odot)	0.0545278(13)

pulsar (Markwardt et al. 2010). The eclipse duration is $\simeq 2065$ s (corresponding to an eclipse half-angle of $\simeq 11.7^\circ$) (Altamirano et al. 2010). Unfortunately, no optical counterpart has been identified yet, with a 3σ upper limit in the I-band of > 19.6 (Yang et al. 2010).

In this *Letter*, we are investigating the properties of the companion star in the case of both main sequence star (MS) and white dwarf (WD), and trying to obtain the pulsar mass. The calculation details are presented in §2 and §3, and the paper is summarized in §4. Through detail calculations, we find that the companion star could be a main-sequence but cannot be a white dwarf.

2 TO UNDERSTAND THE NATURE OF J1749 BY OBSERVATIONS

It is known from observations that J1749 is similar to other low-mass X-ray binary systems driven by disk accretion (Markwardt & Strohmayer 2010), and the observational facts of J1749 are summarized in Table 1 taken from Altamirano et al. (2010). We assume that the companion star should reach its Roche lobe which is approximated by (Eggleton 1983)

$$R_L = a \times \frac{0.49 \cdot q^{2/3}}{0.69 \cdot q^{2/3} + \ln(1 + q^{1/3})}, \quad (1)$$

where a is the semi-major axis of the system and $q = M_c/M_p$ is the ratio between the companion star and the pulsar masses. Importantly, J1749 is the unique system showing eclipse up-to-date. In such an eclipsing system, from geometrical considerations, R_L is also related to the inclination i and the eclipse half-angle $\phi \simeq 11.7^\circ$ by (Chakrabarty et al. 1993, Altamirano et al. 2010)

$$R_L = a \times \sqrt{\cos^2 i + \sin^2 i \cdot \sin^2 \phi}, \quad (2)$$

where the eccentricity of the system is chose to be zero. With the above two equations, we can obtain a rough lower limit of this system according to $\ln(1 + q^{1/3}) > 0$, which is about $i > 46^\circ$, and we will then consider only large inclination angles in this paper.

As we all known that the information of the orbital inclination of binary system is crucial to understanding the properties of its member stars. Unfortunately, determining the inclination is a fantastically difficult work. Fortunately, for the case of eclipsing J1749 system, with the assumption that the radius of the companion star has reached its Roche lobe, we can investigate the relation between the mass of pulsar, M_p and the radius of the companion star, R_c (namely, R_L). This relation can be obtained as follow. According to Eq. (1) and Eq. (2), with different fixed i , there will be different q . Additionally, the Kelper's third law is

$$a = \left[\frac{G(M_p + M_c)P_{\text{orb}}^2}{4\pi^2} \right]^{\frac{1}{3}} = 1.47716[x(1 + q)]^{\frac{1}{3}} R_\odot, \quad (3)$$

where $P_{\text{orb}} = 8.82$ hr is the orbital period of J1749 system, $x = M_p/M_\odot$ is the mass of pulsar in unit of solar mass and R_\odot is radius of the sun. With certain i and equations (2) and (3), the relation between the mass of pulsar and the radius of the companion star is obtained.

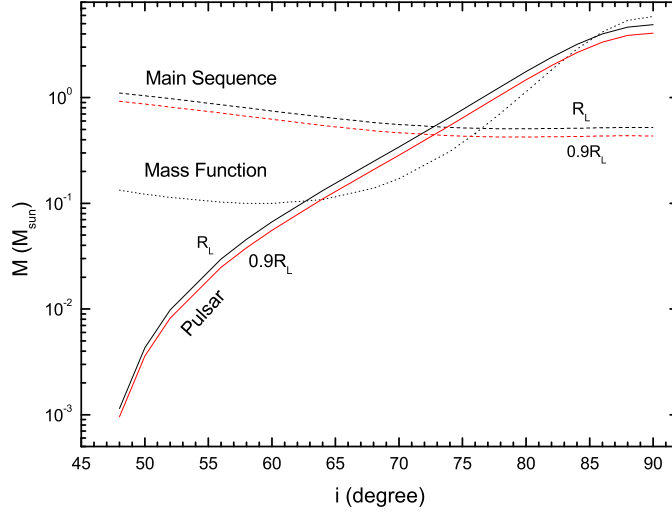


Fig. 1 The masses of both pulsar (solid lines) and its companion (dashed lined) as function of orbital inclination angle. The constraint from the mass function is also drawn (dotted lines). Two cases that the companion reaches its Roche lobe ($R_{\text{MS}} = R_L$) or not ($R_{\text{MS}} = 0.9R_L$) are considered. In this plot, the companion star is assumed to be a MS.

Another consideration comes from the mass-radius relation of companion star, which is empirically given for ZAMSs (zero-age main-sequences) as (Schmidt-Kaler 1982)

$$\log\left(\frac{R}{R_\odot}\right) = 0.640 \log\left(\frac{M}{M_\odot}\right) + 0.011 \quad (0.12 < \log\left(\frac{M}{M_\odot}\right) < 1.3), \quad (4)$$

$$\log\left(\frac{R}{R_\odot}\right) = 0.917 \log\left(\frac{M}{M_\odot}\right) - 0.020 \quad (-1.0 < \log\left(\frac{M}{M_\odot}\right) < 0.12). \quad (5)$$

The above mass-radius relation for ZAMS is consistent with the statistical results presented by Demircan & Kahraman (1991). What we are interested in is the intersection points of R_L and the radius determined by the above mass-radius relation with fixed inclination angle. It is very meaningful to find out all of these intersection points with available inclination angles in order to constrain on properties of both the pulsar and the companion star. The result is showed in Fig. 1.

The third constraint for the companion star comes from the measured mass function of pulsar. The mass function for binary system is (Altamirano et al. 2010)

$$f_p = \frac{(M_c \sin i)^3}{(M_p + M_c)^2} = 0.0545278 M_\odot. \quad (6)$$

Because of unknowing about the orbital inclination, the mass function sets only the minimum companion mass. Nonetheless, if we cover all of the available inclination angle, the measured mass function could give another constraint of the companion star. Combining this constraint and that from previous geometrical consideration, we may obtain unique mass ratio q and thus the companion mass, as well as the inclination angle. The resulting curve is also plotted in Fig. 1 for MSs. We can see in Fig. 1 only one intersection point exists between the mass function curve and the Roche curve, which means that the companion star could be a MS with mass of $M_c \simeq 0.512 M_\odot$. Consequently, the mass of the pulsar is $M_p \simeq 0.989 M_\odot$ and the orbital inclination angle is $i \simeq 76.5^\circ$.

The above calculation is based on the assumption that the radius of the companion star equals to its Roche radius. Keep in mind that for an evolving MS star, its radius will be a little bit larger than that

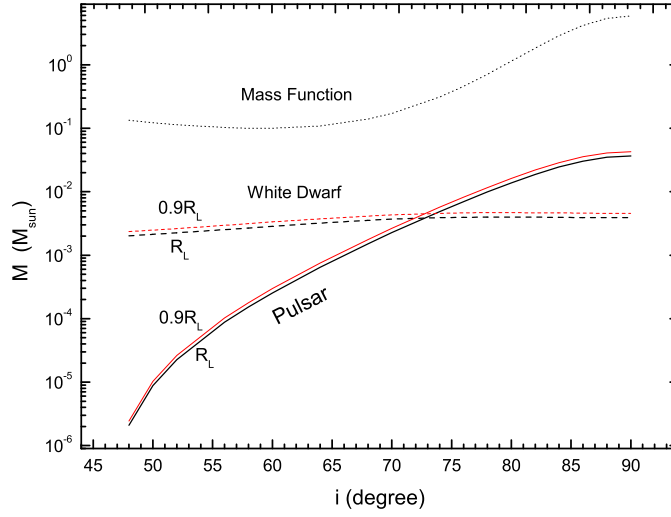


Fig. 2 Same as in Fig. 1, but for white dwarf companion.

of a ZAMS at the same age. This means that the actual radius of the companion star is a little bit larger than the Roche lobe, R_L . Because of this, calculation that the radius of the ZAMS companion star is a little bit smaller than its Roche lobe is necessary. In our calculation we chose that the radius of the companion star is about 90% of its Roche one, namely $R_c = 0.9R_L$. The corresponding curve is also plotted in Fig. 1. In this case, we have $M_c \simeq 0.43M_\odot$, $i \simeq 75.7^\circ$ and $M_p \simeq 0.715M_\odot$.

We also did the same calculation for the case of a WD companion, whose the mass-radius relation is (Shapiro & Teukolsky 1983)

$$M = 0.7011 \left(\frac{R}{10^4 \text{ km}} \right)^{-3} \left(\frac{\mu_e}{2} \right)^{-5} M_\odot, \quad (7)$$

where $\mu_e = A/Z$ is the mean molecular weight per electron. For He-WDs and CO-WDs, μ_e is about 2. Rewriting equation (7), we have

$$R_{\text{WD}} = 0.0161846 R_\odot \left(\frac{M_{\text{WD}}}{M_\odot} \right)^{-1/3} = 0.0161846 (qx)^{-1/3} R_\odot. \quad (8)$$

The result is showed in Fig. 2. From Fig. 2, we can see that there is no interseption between the mass function curve and the Roche curve of WD, which means that WD can be ruled out as the candidate for the companion star.

3 CONSTRAINT ON THE EQUATION OF STATE OF COMPACT STARS

Once obtaining the mass information of the pulsar J1749, one may investigate the nature of pulsar, namely a neutron or quark star. Different equation of state (EoS) can result in different mass-radius relations, and we may calculate the Keplerian frequencies of J1749 in various EoS models. In Newtonian gravity, the Keplerian frequency of the pulsar is gave by

$$\Omega_K = \sqrt{\frac{GM_p}{R^3}} = 11549.9 \sqrt{\frac{x}{r^3}} \text{ s}^{-1}, \quad (9)$$

where G is the gravitational constant, $x = M_p/M_\odot$ and $r = R/(10^6 \text{ cm})$. The mass-radius relations resulted from typical EoSs are showed in Lattimer (2007, Fig. 2 there), and the calculated Keplerian frequencies in typical neutron star model are listed in Table 2.

Table 2 The Kelper frequency Ω_K of the pulsar J1749 under the assumption that both $R_c = R_L$ and $R_c = 0.9R_L$ for a MS companion. The angular frequency is fixed to be $\Omega = 3254.06 \text{ s}^{-1}$. Pulsar's radii for different EoSs are took from Lattimer (2007).

	$R_c = R_L, M_p = 0.989M_\odot$			$R_c = 0.9R_L, M_p = 0.715M_\odot$		
EoS	$R/(10 \text{ km})$	$\Omega_K (\text{s}^{-1})$	Ω/Ω_K	$R/(10 \text{ km})$	$\Omega_K (\text{s}^{-1})$	Ω/Ω_K
MS0	1.471	6438.42	0.505413	1.457	5554.85	0.585805
MS2	1.432	6703.22	0.485447	1.417	5791.71	0.561848
PAL1	1.4	6934.35	0.469267	1.403	5878.61	0.553542
FSU	1.325	7531.37	0.432067	1.368	6105.66	0.532958
PAL6	1.225	8472.15	0.384089	1.3	6590.93	0.493718
MPA1	1.225	8472.15	0.384089	1.218	7267.59	0.447749
AP3	1.2	8738.28	0.372391	1.189	7535.09	0.431854
AP4	1.139	9449.58	0.34436	1.143	7994.52	0.407037
SQM1	0.986	11732.3	0.277359	0.889	11654.9	0.279201
SQM3	0.829	15218.3	0.213825	0.736	15471.9	0.21032

Table 3 The deduced parameters of the J1749 system.

	$R_c = R_L$	$R_c = 0.9R_L$
i	76.5°	75.7°
$R_c(R_\odot)$	0.517	0.440
$M_c(M_\odot)$	0.512	0.430
$M_p(M_\odot)$	0.989	0.715
$B(\text{G})$	$\sim 10^7$	$\sim 10^7$

According to general relativity, the rotation-mode (i.e., r -mode) instability could be excited in fast relativistic stars and they may spin down effectively through radiating gravitational wave (Andersson et al. 2009). Certainly it depends on detail EoS and micro-physics about viscosity to determine the r -mode instability window. Nevertheless, one could calculate a critical angular frequency as a function of temperature, $\Omega_c(T)$, in certain star models. The low limit of of critical frequency could be $< 0.1\Omega_K$ (Andersson et al. 2009), and the pulsar J1749 could be a quark star if the critical frequency is higher than $\sim 0.3\Omega_K$ according to Table 2, since quark stars can sustain faster spin than neutron stars.

4 CONCLUSIONS AND DISCUSSIONS

According to our calculations, we address that the companion star should be a MS with $\sim 0.5M_\odot$ and the inclination angle is about 76° . Assuming a distance of 7 kpc, the peak outburst luminosity was about $1.8 \times 10^{36} \text{ erg/s}$ (Ferrigno et al. 2010). The pulsar accretes matter from its MS companion star, and we can estimate the timescale of this accreting system to be order of 10^9 yr .

Under the assumption that the companion star has reached its Roche lobe, with the observed mass function and the mass-radius relations of both MS and WD, we investigate all of the possible solutions of available inclination angle as well as the corresponding companion star and pulsar masses. All the results are presented in Table 3. The pulsar mass is $\simeq 1.0M_\odot$ which is about the same as the lowest one determined up-to-date, SMC X-1, which is $1.06^{+0.11}_{-0.10}M_\odot$ (van der Meer et al. 2007). According to the mass of the MS companion, we predict the luminosity of the binary system is $\sim 0.09L_\odot$ in optical band, and we expect to detect the companion by the following up observations.

From Garcia et al. (2001, Fig. 1), the minimum luminosity of J1749 should be the order of $10^{-5}L_{\text{Edd}}$, namely $10^{33} \text{ erg s}^{-1}$. One possible reason that J1749 becomes undetectable by *Chandra*¹ could be that the pulsar is now in a propeller phase, and we could then estimate the magnetic field of the pulsar. The pulsar may manifest itself as transient X-ray source if the magnetospheric radius is

¹ Private communication with D. Altamirano.

approaching the corotation radius. The magnetospheric radius is

$$r_m = \left(\frac{B^2 R^6}{\dot{M} \sqrt{2GM_p}} \right)^{2/7} \simeq 1.3 \times 10^{11} \mu_{30}^{4/7} (\dot{M}_{10})^{-2/7} \left(\frac{M_p}{M_\odot} \right)^{-1/7} \text{ cm}, \quad (10)$$

where $\mu_{30} = \mu / (10^{30} \text{ G cm}^3)$ is the magnetic momentum ($\mu = BR^3/2$) in unit of 10^{30} G cm^3 , and $\dot{M}_{10} = \dot{M} / (10^{10} \text{ g s}^{-1})$ is the accretion rate in unit of 10^{10} g s^{-1} . The corotation radius is given by

$$r_{co} = \left(\frac{GM_p}{4\pi^2} \right)^{1/3} P^{2/3} \simeq 1.5 \times 10^8 \left(\frac{M_p}{M_\odot} \right)^{1/3} P^{2/3} \text{ cm}. \quad (11)$$

From $r_m \sim r_{co}$, we could estimate the magnetic field of J1749 to be

$$B \sim 1.45 \times 10^7 \left(\frac{M_p}{M_\odot} \right)^{5/6} \dot{M}_{10}^{1/2} P^{7/6} R_6^{-3} \sim 1 \times 10^7 R_6^{-3} \text{ G}, \quad (12)$$

where $R_6 = R / (10^6 \text{ cm})$. Therefore, J1749 may have relatively weak surface magnetic field.

An accretion-driven millisecond pulsar with $\sim 1M_\odot$ mass would have profound implications to neutron star physics. Millisecond pulsars are supposed to be more massive than normal pulsars in the conventional recycling scenario. However, the mass of J1749 is much lower than the generally accepted pulsar mass $\sim 1.4M_\odot$. A similar case of another accreting and relatively low mass compact star, EXO 0748-676, was also discussed in Xu (2003). These facts may also challenge the standard model for the origin and evolution of millisecond pulsars, besides the arguments from population synthesis (Lorimer et al. 2007). Additionally, considering the r -mode instability, we also estimate the ratio of the real angular frequency to the critical angular frequency, and find that neutron stars could hardly spin so fast (spin period $\sim 2 \text{ ms}$) but quark stars can due to self-confinement and solidification (Xu 2005).

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